

## CHECK YOUR GRASP

## STATISTICS

## EXERCISE-I

## Arithmetic mean, weighted mean, Combined mean

1. Mean of the first  $n$  terms of the A.P.  $a, (a + d), (a + 2d), \dots$  is-
- (1)  $a + \frac{nd}{2}$  (2)  $a + \frac{(n-1)d}{2}$   
 (3)  $a + (n-1)d$  (4)  $a + nd$
2. The A.M. of first  $n$  even natural number is -
- (1)  $n(n+1)$  (2)  $\frac{n+1}{2}$  (3)  $\frac{n}{2}$  (4)  $n+1$
3. The A.M. of  ${}^nC_0, {}^nC_1, {}^nC_2, \dots, {}^nC_n$  is -
- (1)  $\frac{2^n}{n}$  (2)  $\frac{2^{n+1}}{n}$  (3)  $\frac{2^n}{n+1}$  (4)  $\frac{2^{n+1}}{n+1}$
4. If the mean of numbers 27, 31, 89, 107, 156 is 82, then the mean of numbers 130, 126, 68, 50, 1 will be-
- (1) 80 (2) 82 (3) 75 (4) 157
5. If the mean of  $n$  observations  $x_1, x_2, \dots, x_n$  is  $\bar{x}$ , then the sum of deviations of observations from mean is :-
- (1) 0 (2)  $n\bar{x}$   
 (3)  $\frac{\bar{x}}{n}$  (4) None of these
6. The mean of 9 terms is 15. if one new term is added and mean become 16, then the value of new term is :-
- (1) 23 (2) 25 (3) 27 (4) 30
7. If the mean of first  $n$  natural numbers is equal to  $\frac{n+7}{3}$ , then  $n$  is equal to-
- (1) 10 (2) 11  
 (3) 12 (4) none of these
8. The mean of first three terms is 14 and mean of next two terms is 18. The mean of all the five terms is-
- (1) 15.5 (2) 15.0 (3) 15.2 (4) 15.6
9. If the mean of five observations  $x, x+2, x+4, x+6$  and  $x+8$  is 11, then the mean of last three observations is-
- (1) 11 (2) 13 (3) 15 (4) 17
10. The mean of a set of numbers is  $\bar{x}$ . If each number is decreased by  $\lambda$ , the mean of the new set is-
- (1)  $\bar{x}$  (2)  $\bar{x} + \lambda$  (3)  $\lambda - \bar{x}$  (4)  $\bar{x} - \lambda$
11. The mean of 50 observations is 36. If its two observations 30 and 42 are deleted, then the mean of the remaining observations is-
- (1) 48 (2) 36  
 (3) 38 (4) none of these
12. In a frequency dist., if  $d_i$  is deviation of variates from a number  $\ell$  and mean  $= \ell + \frac{\sum f_i d_i}{\sum f_i}$ , then  $\ell$  is :-
- (1) Lower limit (2) Assumed mean  
 (3) Number of observation (4) Class interval
13. The A.M. of  $n$  observation is  $\bar{x}$ . If the sum of  $n-4$  observations is  $K$ , then the mean of remaining observations is-
- (1)  $\frac{\bar{x}-K}{4}$  (2)  $\frac{n\bar{x}-K}{n-4}$   
 (3)  $\frac{n\bar{x}-K}{4}$  (4)  $\frac{n\bar{x}-(n-4)K}{4}$
14. The mean of values  $1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}$  which have frequencies 1, 2, 3,  $\dots, n$  resp., is :-
- (1)  $\frac{2n+1}{3}$  (2)  $\frac{2}{n}$  (3)  $\frac{n+1}{2}$  (4)  $\frac{2}{n+1}$
15. The sum of squares of deviation of variates from their A.M. is always :-
- (1) Zero (2) Minimum  
 (3) Maximum (4) Nothing can be said
16. If the mean of following freq. dist. is 2.6, then the value of  $f$  is :-
- |       |   |   |     |   |   |
|-------|---|---|-----|---|---|
| $x_i$ | 1 | 2 | 3   | 4 | 5 |
| $f_i$ | 5 | 4 | $f$ | 2 | 3 |
- (1) 1 (2) 3  
 (3) 8 (4) None of these
17. The weighted mean (W.M.) is computed by the formula ?
- (1)  $W.M. = \frac{\sum x_i}{\sum w_i}$  (2)  $W.M. = \frac{\sum w_i}{\sum x_i}$   
 (3)  $W.M. = \frac{\sum w_i x_i}{\sum x_i}$  (4)  $W.M. = \frac{\sum w_i x_i}{\sum w_i}$
18. The weighted mean of first  $n$  natural numbers when their weights are equal to corresponding natural number, is :-
- (1)  $\frac{n+1}{2}$  (2)  $\frac{2n+1}{3}$   
 (3)  $\frac{(n+1)(2n+1)}{6}$  (4) None of these
19. The average income of a group of persons is  $\bar{x}$  and that of another group is  $\bar{y}$ . If the number of persons of both group are in the ratio 4 : 3, then average income of combined group is :-
- (1)  $\frac{\bar{x} + \bar{y}}{7}$  (2)  $\frac{3\bar{x} + 4\bar{y}}{7}$   
 (3)  $\frac{4\bar{x} + 3\bar{y}}{7}$  (4) None of these

20. In a group of students, the mean weight of boys is 65 kg. and mean weight of girls is 55 kg. If the mean weight of all students of group is 61 kg, then the ratio of the number of boys and girls in the group is :-

(1) 2 : 3      (2) 3 : 1      (3) 3 : 2      (4) 4 : 3

**Geometric mean, Harmonic mean**

21. The G.M. of  $n$  positive terms  $x_1, x_2, \dots, x_n$  is :-

(1)  $(x_1 \cdot x_2 \cdot \dots \cdot x_n)^{1/n}$       (2)  $\frac{1}{n}(x_1 + x_2 + \dots + x_n)$

(3)  $(x_1 \cdot x_2 \cdot \dots \cdot x_n)^{1/n}$       (4) None of these

22. The G.M. of numbers 4, 5, 10, 20, 25 is :-

(1) 12.8      (2) 10  
(3) 7.8      (4) None of these

23. The geometric mean of the first  $n$  terms of the series  $a, ar, ar^2, \dots$ , is-

(1)  $ar^{n/2}$       (2)  $ar^n$       (3)  $ar^{(n-1)/2}$       (4)  $ar^{n-1}$

24. If  $G_1$  and  $G_2$  are geometric mean of two series of sizes  $n_1$  and  $n_2$  resp. and  $G$  is geometric mean of their combined series, then  $\log G$  is equal to :-

(1)  $\log G_1 + \log G_2$       (2)  $n_1 \log G_1 + n_2 \log G_2$

(3)  $\frac{\log G_1 + \log G_2}{n_1 + n_2}$       (4)  $\frac{n_1 \log G_1 + n_2 \log G_2}{n_1 + n_2}$

25. The Harmonic mean of 3, 7, 8, 10, 14 is-

(1)  $\frac{3+7+8+10+14}{5}$

(2)  $\frac{5}{3+7+8+10+14}$

(3)  $\frac{\frac{1}{3} + \frac{1}{7} + \frac{1}{8} + \frac{1}{10} + \frac{1}{14}}{5}$

(4)  $\frac{5}{\frac{1}{3} + \frac{1}{7} + \frac{1}{8} + \frac{1}{10} + \frac{1}{14}}$

26. The H.M. of the numbers 2, 3, 4 is :-

(1) 3      (2)  $2(3)^{1/3}$       (3)  $\frac{36}{13}$       (4)  $\frac{13}{36}$

27. The H.M. of following freq. dist. is :-

$x_i$	3	6	9	12
$f_i$	1	2	3	4

(1) 9      (2) 3  
(3) 7.5      (4) None of these

28. A boy goes to school from his home at a speed of  $x$  km/hr. and comes back at a speed of  $y$  km/hr. then the average speed of the boy is :-

(1)  $\frac{x+y}{2}$  km/hr      (2)  $\sqrt{xy}$  km/hr

(3)  $\frac{2xy}{x+y}$  km/hr      (4)  $\frac{x+y}{2xy}$  km/hr

**Median, Mode**

29. The median of an arranged series of  $n$  even observations, will be :-

(1)  $\left(\frac{n+1}{2}\right)$ th term

(2)  $\left(\frac{n}{2}\right)$ th term

(3)  $\left(\frac{n}{2}+1\right)$ th term

(4) Mean of  $\left(\frac{n}{2}\right)$ th and  $\left(\frac{n}{2}+1\right)$ th terms

30. The median of the numbers 6, 14, 12, 8, 10, 9, 11, is :-

(1) 8      (2) 10      (3) 10.5      (4) 11

31. Median of the following freq. dist.

$x_i$	3	6	10	12	7	15
$f_i$	3	4	2	8	13	10

(1) 7      (2) 10  
(3) 8.5      (4) None of these

32. Median is independent of change of :-

(1) only Origin  
(2) only Scale  
(3) Origin and scale both  
(4) Neither origin nor scale

33. A series which have numbers three 4's, four 5's, five 6's, eight 7's, seven 8's and six 9's then the mode of numbers is :-

(1) 9      (2) 8      (3) 7      (4) 6

34. Mode of the following frequency distribution

$x$	4	5	6	7	8
$f$	6	7	10	8	3

(1) 5      (2) 6      (3) 8      (4) 10

35. The mode of the following freq. dist is :-

Class	1-10	11-20	21-30	31-40	41-50
$f_i$	5	7	8	6	4

(1) 24      (2) 23.83  
(3) 27.16      (4) None of these

**Symmetric and asymmetric distribution, Range**

36. For a normal dist :-  
 (1) mean = median  
 (2) median = mode  
 (3) mean = mode  
 (4) mean = median = mode
37. The relationship between mean, median and mode for a moderately skewed distribution is-  
 (1) mode = median - 2 mean  
 (2) mode = 2 median - mean  
 (3) mode = 2 median - 3 mean  
 (4) mode = 3 median - 2 mean
38. The range of observations 2, 3, 5, 9, 8, 7, 6, 5, 7, 4, 3 is :-  
 (1) 6 (2) 7 (3) 5.5 (4) 11

**Mean Deviation**

39. The mean deviation of a frequency dist. is equal to :-  
 (1)  $\frac{\sum d_i}{\sum f_i}$  (2)  $\frac{\sum |d_i|}{\sum f_i}$   
 (3)  $\frac{\sum f_i d_i}{\sum f_i}$  (4)  $\frac{\sum f_i |d_i|}{\sum f_i}$
40. Mean deviation from the mean for the observation -1, 0, 4 is-  
 (1)  $\sqrt{\frac{14}{3}}$  (2)  $\frac{2}{3}$   
 (3) 2 (4) none of these
41. Mean deviation of the observations 70, 42, 63, 34, 44, 54, 55, 46, 38, 48 from median is :-  
 (1) 7.8 (2) 8.6  
 (3) 7.6 (4) 8.8
42. Mean deviation of 5 observations from their mean 3 is 1.2, then coefficient of mean deviation is :-  
 (1) 0.24 (2) 0.4  
 (3) 2.5 (4) None of these
43. The mean deviation from median is  
 (1) greater than the mean deviation from any other central value  
 (2) less than the mean deviation from any other central value  
 (3) equal to the mean deviation from any other central value  
 (4) maximum if all values are positive

**Variance and Standard Deviation**

44. The variate  $x$  and  $u$  are related by  $u = \frac{x-a}{h}$  then correct relation between  $\sigma_x$  and  $\sigma_u$  is :-  
 (1)  $\sigma_x = h\sigma_u$  (2)  $\sigma_x = h + \sigma_u$   
 (3)  $\sigma_u = h\sigma_x$  (4)  $\sigma_u = h + \sigma_x$
45. The S.D. of the first  $n$  natural numbers is-  
 (1)  $\sqrt{\frac{n^2-1}{2}}$  (2)  $\sqrt{\frac{n^2-1}{3}}$   
 (3)  $\sqrt{\frac{n^2-1}{4}}$  (4)  $\sqrt{\frac{n^2-1}{12}}$
46. The variance of observations 112, 116, 120, 125, 132 is :-  
 (1) 58.8 (2) 48.8  
 (3) 61.8 (4) None of these
47. If  $\sum_{i=1}^{10} (x_i - 15) = 12$  and  $\sum_{i=1}^{10} (x_i - 15)^2 = 18$  then the S.D. of observations  $x_1, x_2, \dots, x_{10}$  is :-  
 (1)  $\frac{2}{5}$  (2)  $\frac{3}{5}$   
 (3)  $\frac{4}{5}$  (4) None of these
48. The S.D. of 7 scored 1, 2, 3, 4, 5, 6, 7 is-  
 (1) 4 (2) 2  
 (3)  $\sqrt{7}$  (4) none of these
49. The variance of series  $a, a + d, a + 2d, \dots, a + 2nd$  is :-  
 (1)  $\frac{n(n+1)}{2}d^2$  (2)  $\frac{n(n+1)}{3}d^2$   
 (3)  $\frac{n(n+1)}{6}d^2$  (4)  $\frac{n(n+1)}{12}d^2$
50. Variance is independent of change of-  
 (1) only origin  
 (2) only scale  
 (3) origin and scale both  
 (4) none of these

51. If the coefficient of variation and standard deviation of a distribution are 50% and 20 respectively, then its mean is-

- (1) 40 (2) 30  
(3) 20 (4) None of these

52. If each observation of a dist. whose S.D. is  $\sigma$ , is increased by  $\lambda$ , then the variance of the new observations is -

- (1)  $\sigma$  (2)  $\sigma + \lambda$   
(3)  $\sigma^2$  (4)  $\sigma^2 + \lambda$

53. The variance of 2, 4, 6, 8, 10 is-

- (1) 8 (2)  $\sqrt{8}$   
(3) 6 (4) none of these

54. If each observation of a dist., whose variance is  $\sigma^2$ , is multiplied by  $\lambda$ , then the S.D. of the new new observations is-

- (1)  $\sigma$  (2)  $\lambda\sigma$   
(3)  $|\lambda|\sigma$  (4)  $\lambda^2\sigma$

55. The standard deviation of variate  $x_i$  is  $\sigma$ . Then standard deviation of the variate  $\frac{ax_i + b}{c}$ , where  $a, b, c$  are constants is-

- (1)  $\left(\frac{a}{c}\right)\sigma$  (2)  $\left|\frac{a}{c}\right|\sigma$   
(3)  $\left(\frac{a^2}{c^2}\right)\sigma$  (4) None of these

CHECK YOUR GRASP								ANSWER-KEY					EXERCISE-I							
Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Ans.	2	4	3	3	1	2	2	4	2	4	2	2	3	4	2	1	4	2	3	3
Que.	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans.	3	2	3	4	4	3	3	3	4	2	3	4	3	2	2	4	4	2	4	3
Que.	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55					
Ans.	2	2	2	1	4	2	2	2	2	1	1	3	1	3	2					

## BRAIN TEASERS

## STATISTICS

## EXERCISE-II

- The A.M. of the series 1, 2, 4, 8, 16, .....,  $2^n$  is-  
 (1)  $\frac{2^n - 1}{n}$  (2)  $\frac{2^{n+1} - 1}{n+1}$   
 (3)  $\frac{2^n - 1}{n+1}$  (4)  $\frac{2^{n+1} - 1}{n}$
- If the mean of  $n$  observations  $1^2, 2^2, 3^2, \dots, n^2$  is  $\frac{46n}{11}$ , then  $n$  is equal to-  
 (1) 11 (2) 12  
 (3) 23 (4) 22
- The weighted mean of first  $n$  natural numbers whose weights are equal, is :-  
 (1)  $\frac{n+1}{2}$  (2)  $\frac{2n+1}{2}$   
 (3)  $\frac{2n+1}{3}$  (4)  $\frac{(2n+1)(n+1)}{6}$
- The average age of a group of men and women is 30 years. If average age of men is 32 and that of women is 27, then the percentage of women in the group is-  
 (1) 60 (2) 50  
 (3) 40 (4) 30
- The geometric mean of the observations 2, 4, 8, 16, 32, 64 is-  
 (1)  $2^{5/2}$  (2)  $2^{7/2}$   
 (3) 33 (4) None of these
- The H.M. of the reciprocal of first  $n$  natural numbers is :-  
 (1)  $\frac{n+1}{2}$  (2)  $\frac{n}{\left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}\right)}$   
 (3)  $\frac{2}{n+1}$  (4) None of these
- Product of  $n$  positive numbers is unit. The sum of these numbers can not be less than-  
 (1) 1 (2)  $n$   
 (3)  $n^2$  (4) none of these
- The A.M. of first  $n$  terms of the series 1.3.5, 3.5.7, 5.7.9, ....., is-  
 (1)  $3n^3 + 6n^2 + 7n - 1$  (2)  $n^3 + 8n^2 + 7n - 1$   
 (3)  $2n^3 + 8n^2 - 7n - 2$  (4)  $2n^3 + 8n^2 + 7n - 2$
- The observations 29, 32, 48, 50,  $x$ ,  $x + 2$ , 72, 78, 84, 95 are arranged in ascending order and their median is 63 then the value of  $x$  is :-  
 (1) 61 (2) 62 (3) 62.5 (4) 63
- If the mode of a distribution is 18 and the mean is 24, then median is-  
 (1) 18 (2) 24 (3) 22 (4) 21
- If the mean and S.D. of  $n$  observations  $x_1, x_2, \dots, x_n$  are  $\bar{x}$  and  $\sigma$  resp, then the sum of squares of observations is :-  
 (1)  $n(\sigma^2 + \bar{x}^2)$  (2)  $n(\sigma^2 - \bar{x}^2)$   
 (3)  $n(\bar{x}^2 - \sigma^2)$  (4) None of these
- The variance of observations 8, 12, 13, 15, 22, is :-  
 (1) 21 (2) 21.2  
 (3) 21.4 (4) None of these
- If the mean of a set of observations  $x_1, x_2, \dots, x_{10}$  is 20, then the mean of  $x_1 + 4, x_2 + 8, x_3 + 12, \dots, x_{10} + 40$  is-  
 (1) 34 (2) 42 (3) 38 (4) 40
- The mean of values 0, 1, 2, .....,  $n$  when their weights are  $1, {}^nC_1, {}^nC_2, \dots, {}^nC_n$ , resp., is  
 (1)  $\frac{2^n}{n+1}$  (2)  $\frac{n+1}{2}$  (3)  $\frac{2^{n+1}}{n(n+1)}$  (4)  $\frac{n}{2}$
- The G.M. of first  $n$  natural numbers is :-  
 (1)  $\frac{n+1}{2}$  (2)  $(n!)^n$   
 (3)  $(n!)^{1/n}$  (4) None of these
- If a variable takes the discrete values  $\alpha + 4, \alpha - \frac{7}{2}, \alpha - \frac{5}{2}, \alpha - 3, \alpha - 2, \alpha + \frac{1}{2}, \alpha - \frac{1}{2}, \alpha + 5$  ( $\alpha > 0$ ), then the median of these values-  
 (1)  $\alpha - \frac{5}{4}$  (2)  $\alpha - \frac{1}{2}$   
 (3)  $\alpha - 2$  (4)  $\alpha + \frac{5}{4}$
- The S.D. of first  $n$  odd natural numbers is :-  
 (1)  $\sqrt{\frac{n^2 - 1}{2}}$  (2)  $\sqrt{\frac{n^2 - 1}{3}}$   
 (3)  $\sqrt{\frac{n^2 - 1}{6}}$  (4)  $\sqrt{\frac{n^2 - 1}{12}}$

18. If the sum and sum of squares of 10 observations are 12 and 18 resp., then, The S.D. of observations is :-

(1)  $\frac{1}{5}$  (2)  $\frac{2}{5}$  (3)  $\frac{3}{5}$  (4)  $\frac{4}{5}$

19. The mean of  $n$  values of a distribution is  $\bar{x}$ . If its first value is increased by 1, second by 2, .... then the mean of new values will be-

(1)  $\bar{x} + n$  (2)  $\bar{x} + n/2$   
(3)  $\bar{x} + \left(\frac{n+1}{2}\right)$  (4) None of these

20. The mean of the series  $x_1, x_2, \dots, x_n$  is  $\bar{X}$ . If  $x_2$  is replaced by  $\lambda$ , then the new mean is-

(1)  $\frac{\bar{X} - x_2 + \lambda}{n}$  (2)  $\frac{n\bar{X} + x_2 - \lambda}{n}$   
(3)  $\frac{(n-1)\bar{X} + \lambda}{n}$  (4)  $\frac{n\bar{X} - x_2 + \lambda}{n}$

21. Let  $G_1$  and  $G_2$  be the geometric means of two series  $x_1, x_2, \dots, x_n$  and  $y_1, y_2, \dots, y_n$  respectively. If  $G$  is the geometric mean of series  $x_i/y_i, i = 1, 2, \dots, n$ , then  $G$  is equal to-

(1)  $G_1 - G_2$  (2)  $\log G_1 / \log G_2$   
(3)  $\log (G_1/G_2)$  (4)  $G_1/G_2$

22. The mean deviation of the numbers 1, 2, 3, 4, 5 is-

(1) 0 (2) 1.2  
(3) 2 (4) 1.4

23. If mean = (3 median - mode)  $x$ , then the value of  $x$  is-

(1) 1 (2) 2 (3)  $1/2$  (4)  $3/2$

24. A man spends equal ammount on purchasing three kinds of pens at the rate 5 Rs/pen, 10 Rs/pen, 20 Rs/pen, then average cost of one pen is :-

(1) 10 Rs (2)  $\frac{35}{3}$  Rs  
(3)  $\frac{60}{7}$  Rs (4) None of these

25. The median of 21 observation is 40. if each observations greater than the median are increased by 6, then the median of the observations will be-

(1) 40 (2) 46  
(3)  $46 + 40/21$  (4)  $46 - 40/21$

26. The coefficient of range of the following distribution 10, 14, 11, 9, 8, 12, 6

(1) 0.4 (2) 2.5  
(3) 8 (4) 0.9

27. The S.D. of the following freq. dist. :-

Class	0 - 10	10 - 20	20 - 30	30 - 40
$f_i$	1	3	4	2

(1) 7.8 (2) 9  
(3) 8.1 (4) 0.9

28. The mean of a dist. is 4. if its coefficient of variation is 58%. Then the S.D. of the dist. is :-

(1) 2.23 (2) 3.23  
(3) 2.32 (4) None of these

29. The mean of a set of observations is  $\bar{x}$ . If each observation is divided by  $\alpha$ , ( $\alpha \neq 0$ ) and then is increased by 10, then the mean of the new set is

(1)  $\frac{\bar{x}}{\alpha}$  (2)  $\frac{\bar{x} + 10}{\alpha}$   
(3)  $\frac{\bar{x} + 10\alpha}{\alpha}$  (4)  $\frac{\alpha\bar{x} + 10}{\alpha}$

30. The average age of a teacher and three students is 20 years. If all students are of equal age and the difference between the age of the teacher and that of a student is 20 years, then the age of the teacher is-

(1) 25 years (2) 30 years  
(3) 35 years (4) 45 years

31. If  $a, b, c$  are any three positive numbers, then the least value of  $(a + b + c) \left( \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right)$  is-

(1) 3 (2) 6  
(3) 9 (4) None of these

32. Median of  ${}^{2n}C_0, {}^{2n}C_1, {}^{2n}C_2, \dots, {}^{2n}C_n$  (when  $n$  is even) is-

(1)  ${}^{2n}C_{\frac{n-1}{2}}$  (2)  ${}^{2n}C_{\frac{n}{2}}$   
(3)  ${}^{2n}C_{\frac{n+1}{2}}$  (4) None of these

33. The mean deviation from mean of observations 5, 10, 15, 20, .....85 is :-

(1) 43.71 (2) 21.17  
(3) 38.7 (4) None of these

34. If standard deviation of variate  $x_i$  is 10, then variance of the variate  $(50 + 5x_i)$  will be-

(1) 50 (2) 250  
(3) 500 (4) 2500

35. The S.D. of the numbers 31, 32, 33, .... 47 is-
- (1)  $2\sqrt{6}$  (2)  $4\sqrt{3}$
- (3)  $\sqrt{\frac{47^2-1}{12}}$  (4) None of these
36. The sum of the squares of deviation of 10 observations from their mean 50 is 250, then coefficient of variation is-
- (1) 10% (2) 40%
- (3) 50% (4) None of these
37. The median and standard deviation (S.D.) of a distribution will be, If each term is increased by 2 -
- (1) median and S.D. will increased by 2
- (2) median will increased by 2 but S.D. will remain same
- (3) median will remain same but S.D. will increased by 2
- (4) median and S.D. will remain same
38. If  $\bar{X}_1$  and  $\bar{X}_2$  are the means of two series such that  $\bar{X}_1 < \bar{X}_2$  and  $\bar{X}$  is the mean of the combined series, then-
- (1)  $\bar{X} < \bar{X}_1$  (2)  $\bar{X} > \bar{X}_2$
- (3)  $\bar{X}_1 < \bar{X} < \bar{X}_2$  (4)  $\bar{X} = \frac{\bar{X}_1 + \bar{X}_2}{2}$
39. The median of 19 observations of a group is 30. If two observations with values 8 and 32 are further included, then the median of the new group of 21 observation will be
- (1) 28 (2) 30
- (3) 32 (4) 34
40. The coefficient of mean deviation from median of observations 40, 62, 54, 90, 68, 76 is :-
- (1) 2.16 (2) 0.2
- (3) 5 (4) None of these
41. A group of 10 observations has mean 5 and S.D.  $2\sqrt{6}$ . another group of 20 observations has mean 5 and S.D.  $3\sqrt{2}$ , then the S.D. of combined group of 30 observations is :-
- (1)  $\sqrt{5}$  (2)  $2\sqrt{5}$
- (3)  $3\sqrt{5}$  (4) None of these
42. For the values  $x_1, x_2, \dots, x_{101}$  of a distribution  $x_1 < x_2 < x_3 < \dots < x_{100} < x_{101}$ . The mean deviation of this distribution with respect to a number k will be minimum when k is equal to-
- (1)  $x_1$  (2)  $x_{51}$
- (3)  $x_{50}$  (4)  $\frac{x_1 + x_2 + \dots + x_{101}}{101}$
43. In any discrete series (when all the value are not same) the relationship between M.D. about mean and S.D. is-
- (1) M.D. = S.D. (2) M.D. > S.D.
- (3) M.D. < S.D. (4) M.D.  $\leq$  S.D.

BRAIN TEASERS								ANSWER-KEY					EXERCISE-II							
Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Ans.	2	1	1	3	2	3	2	4	2	3	1	2	2	4	3	1	2	3	3	4
Que.	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
Ans.	4	2	3	3	1	1	2	3	3	3	3	2	2	4	1	1	2	3	2	2
Que.	41	42	43																	
Ans.	2	2	3																	

**PREVIOUS YEAR QUESTIONS**

**STATISTICS**

**EXERCISE-III**

- The mean of Mathematics marks of 100 students of a class is 72. If the number of boys is 70 and the mean of their marks is 75. Then the mean of the marks of girls in the class will be- [AIEEE-2002]  
(1) 60 (2) 62 (3) 65 (4) 68
- In an experiment with 15 observations of  $x$ , the following results were available  $\sum x^2 = 2830$ ,  $\sum x = 170$ . One observation that was 20 was found to be wrong and it was replaced by its correct value 30. Then the corrected variance is- [AIEEE-2003]  
(1) 8.33 (2) 78 (3) 188.66 (4) 177.33
- The mean and variance of a random variable  $X$  having a binomial distribution are 4 and 2 respectively. Then  $P(X = 1)$  is- [AIEEE-2003]  
(1)  $\frac{1}{4}$  (2)  $\frac{1}{32}$  (3)  $\frac{1}{16}$  (4)  $\frac{1}{8}$
- The median of a set of 9 distinct observations is 20.5. If each of the largest four observations of the set is increased by 2, then the median of the new set- [AIEEE-2003]  
(1) remains the same as that of the original set  
(2) is increased by 2  
(3) is decreased by 2  
(4) is two times the original median
- Consider the following statements- [AIEEE-2004]  
(a) Mode can be computed from histogram  
(b) median is not independent of change of scale  
(c) variance is independent of change of origin and scale  
which of these are correct-  
(1) only (a) and (b) (2) only (b)  
(3) only (a) (4) (a), (b) and (c)
- In a series of  $2n$  observations, half of them equal  $a$  and remaining half equal  $-a$ . If the standard deviation of the observations is 2, then  $|a|$  equals- [AIEEE-2004]  
(1) 2 (2)  $\sqrt{2}$  (3)  $\frac{1}{n}$  (4)  $\frac{\sqrt{2}}{n}$
- The mean and the variance of a binomial distribution are 4 and 2 respectively. Then the probability of 2 successes is- [AIEEE-2004]  
(1)  $\frac{128}{256}$  (2)  $\frac{219}{256}$  (3)  $\frac{37}{256}$  (4)  $\frac{28}{256}$

- If in a frequency distribution, the mean and median are 21 and 22 respectively, then its mode is approximately- [AIEEE-2005]  
(1) 24.0 (2) 25.5  
(3) 20.5 (4) 22.0
- Let  $x_1, x_2, \dots, x_n$  be  $n$  observations such that  $\sum x_i^2 = 400$  and  $\sum x_i = 80$ . Then a possible value of  $n$  among the following is- [AIEEE-2005]  
(1) 12 (2) 9 (3) 18 (4) 15
- Suppose a population A has 100 observations 101, 102, ..., 200 and other population B has 100 observations 151, 152, ..., 250. If  $V_A$  and  $V_B$  represent the variance of two population respectively then  $\frac{V_A}{V_B}$  is- [AIEEE-2006]  
(1)  $\frac{9}{4}$  (2)  $\frac{4}{9}$  (3)  $\frac{2}{3}$  (4) 1
- The average marks of boys in a class 52 and that of girls is 42. The average marks of boys and girls combined is 50 then the percentage of boys in the class is- [AIEEE-2007]  
(1) 20 (2) 80 (3) 60 (4) 40
- The mean of the numbers  $a, b, 8, 5, 10$  is 6 and the variance is 6.80 then which one of the following gives possible values of  $a$  and  $b$ ? [AIEEE-2008]  
(1)  $a = 0, b = 7$  (2)  $a = 5, b = 2$   
(3)  $a = 1, b = 6$  (4)  $a = 3, b = 4$
- Statement-1 :**  
The variance of first  $n$  even natural numbers is  $\frac{n^2 - 1}{4}$ .  
**Statement-2 :**  
The sum of first  $n$  natural numbers is  $\frac{n(n+1)}{2}$  and the sum of squares of first  $n$  natural numbers is  $\frac{n(n+1)(2n+1)}{6}$ . [AIEEE-2009]  
(1) Statement-1 is true, Statement-2 is false.  
(2) Statement-1 is false, Statement-2 is true.  
(3) Statement-1 is true, Statement-2 is true ; Statement-2 is a correct explanation for Statement-1.  
(4) Statement-1 is true, Statement-2 is true ; Statement-2 is not a correct explanation for statement-1.



14. If the mean deviation of the numbers  $1, 1 + d, 1 + 2d, \dots, 1 + 100d$  from their mean is 255, then that  $d$  is equal to :- [AIEEE-2009]  
 (1) 10.1 (2) 20.2 (3) 10.0 (4) 20.0

15. For two data sets each of size is 5, the variances are given to be 4 and 5 and the corresponding means are given to be 2 and 4 respectively, then the variance of the combined data set is :- [AIEEE-2010]  
 (1)  $\frac{5}{2}$  (2)  $\frac{11}{2}$  (3) 6 (4)  $\frac{13}{2}$

16. If the mean deviation about the median of the numbers  $a, 2a, \dots, 50a$  is 50, then  $|a|$  equals:- [AIEEE-2011]  
 (1) 4 (2) 5 (3) 2 (4) 3

17. A scientist is weighing each of 30 fishes. Their mean weight worked out is 30 gm and a standard deviation of 2 gm. Later, it was found that the measuring scale was misaligned and always under reported every fish weight by 2 gm. The correct mean and standard deviation (in gm) of fishes are respectively : [AIEEE-2011]  
 (1) 28, 4 (2) 32, 2 (3) 32, 4 (4) 28, 2

18. Let  $x_1, x_2, \dots, x_n$  be  $n$  observations, and let  $\bar{x}$  be their arithmetic mean and  $\sigma^2$  be their variance.

**Statement-1** : Variance of  $2x_1, 2x_2, \dots, 2x_n$  is  $4\sigma^2$ .

**Statement-2** : Arithmetic mean of

$2x_1, 2x_2, \dots, 2x_n$  is  $4\bar{x}$ . [AIEEE-2012]

- (1) Statement-1 is true, Statement-2 is false.  
 (2) Statement-1 is false, Statement-2 is true.  
 (3) Statement-1 is true, Statement-2 is true ; Statement-2 is a correct explanation for Statement-1.  
 (4) Statement-1 is true, Statement-2 is true ; Statement-2 is not a correct explanation for Statement-1.

PREVIOUS YEARS QUESTIONS						ANSWER-KEY				EXERCISE-III					
Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans	3	2	2	1	1	1	4	1	3	4	2	4	2	1	2
Que.	16	17	18												
Ans	1	2	1												